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# **Stability and Robustness Considerations in Nonlinear Model Predictive Control**

Reihe **8**: Meß-, Steuerungs-  
und Regelungstechnik

Nr. **674**

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